## Thin films analysis

XRR GIXRD In-Plane diffraction HR-XRD



#### What XRD reveals





#### **XRD scan modes**

method	scan axes	purpose	
Out-of-plane	2θ/ω	Qualitative analysis, crystal structure reflectivity	
Thin film scan	20	Qualitative analysis, crystal structure	
In-plane	2θχ/φ	Qualitative analysis, crystal structure	
Pole figure	<b>χ(α), φ(β)</b>	Preferred orientation	
Rocking curve	ω, χ, φ	Preferred orientation, crystal perfection	
Rocking curve (high resolution)	2θ/ω	Crystal perfection, film thickness, composition rate	
Reciprocal lattice map	2θ/ω, ω	Crystal perfection, epitaxial relationship analysis	



#### Wide angle XRD





#### **XRD scan modes: Comparison**





## $2\theta/\omega$ scan (out-of-plane)

- Diffraction patterns contributed by the planes parallel to the sample surface are observed.
  - Qualitative analysis
  - Preferred orientation









#### $\theta$ -2 $\theta$ scan





## 2θ scan (thin film XRD)

- XRD patterns from the sample surface layers are obtained.
  - Qualitative analysis for thin films (suitable for the case of random orientation)







#### $\omega$ -fixed 2 $\theta$ scan





## 2θχ/φ scan (in-plane)

- Diffraction patterns contributed by the planes perpendicular to the sample surface are obtained.
  - Qualitative analysis for thin films
  - Preferred orientation







#### **In-Plane measurement**





#### **In-Plane XRD**



Sample is always mounted on horizontal plane.

## "3D"s for In-Plane diffraction



**Direct observation** of lattice planes normal to surface utilizing total external reflection of X-rays



**Depth analysis** through small incident angle non-destructive analysis of depth-variation (d-values, crystallite-size, reaction layer, etc.)



Detection of minor phases surface-sensitive even weak signals can be effectively collected



## Important point for In-Plane diffraction

©Divergence of Incident X-ray along surface normal direction





#### incident angle vs penetration depth



Incident angle(deg.)



#### Sample alignment for In-plane measurement

- To keep the incident angle constant during a scan





#### **Rocking curve measurement**

- tilting :  $\omega$  scan with fixed 2 $\theta$ . (Out-of-plane)
- twisting :  $\phi$  scan with fixed  $2\theta\chi$ . (In-plane)





#### tilting **@ Rigaku**

# X-ray Residual Stress Measurement



## What is Residual Stress

- Residual stresses are internal stresses remaining in materials after the external force is removed. The residual stress plays important role in the processes of elastic and plastic deformations, material hardness and plasticity, material damages and other processes related to physical and mechanical properties of solid state
- In the equilibrium condition, the **sum of residual stresses** in the sample must be equal zero
- There are negative (compressive) and positive (tensile) stresses
- The residual stresses are observed in polycrystalline materials and single crystals
- In single crystals or epitaxial films, usually the "language of strains" is used instead of "stress"
- In polycrystals, the residual stress exists in most of solid state samples
- Stress is related to strain via **Hook's law**



## **Origin of stress**

- Inhomogeneous plastic deformations: rolling, grinding, polishing
- Microscopic transformations: dislocations, stacking faults, defects, twins
- Thermal incompatibility
- Phase transitions
- Hardening processes (quenching, laser treatment, thermal heating)
- Implantations, for example ion-implanted semiconductors
- Deformation
- Recrystallization
- Film synthesis with plasma, laser and ion beams
- Crystallization to boundary surfaces
- ...and many others



## Strain

Strain is a measure of the resulting deformation of a solid body caused by stress. Strain is calculated from the change in the size and shape of the deformed solid due to stress.

For crystalline or polycrystalline materials possessing crystallographic lattice (*a*, *b*, *c*), the strain in the selected direction *a* is defined:

$$\varepsilon_a = \frac{a - a_0}{a_0}$$

Strain is a measure of displacement of crystallographic lattice and reflects the stress status of the lattice. In coherent structures (perfect crystals, epitaxy), the strain is also related to lattice **mismatch** 

![](_page_20_Picture_6.jpeg)

![](_page_20_Picture_7.jpeg)

![](_page_20_Figure_8.jpeg)

### Strain&Stress&Units

![](_page_21_Figure_2.jpeg)

Stress (top) and strain (bottom) components in a volume of the sample

![](_page_21_Figure_4.jpeg)

![](_page_21_Picture_5.jpeg)

Unit for stress: **Pa** (Pascal; measure of force per unit area, N/m<sup>2</sup>).

For most metals, stress is normally given in MPa, which is defined as MN/m<sup>2</sup> (million Newtons per square meters) or equivalently N/mm<sup>2</sup> (newton per square millimeter). Other units:

1 GPa = 1000 MPa 1 ksi (1000 lb/in<sup>2</sup>) = 6.895 MPa 1 kg/mm<sup>2</sup> = 9.807 MPa

## **Randomly Oriented Crystal Grains**

Polycrystalline materials are composed of millions of crystal grains. Residual stress induced in materials with randomly oriented crystal grains only is treated here.

![](_page_22_Figure_3.jpeg)

![](_page_22_Picture_4.jpeg)

X-ray diffraction measures the real lattice constants of crystallographic lattice in crystallites which compose polycrystalline sample. If the lattice is deformed (strained), the Bragg peak is shifted from the position corresponding to relaxed lattice. Thus X-ray Bragg diffraction measures the **lattice strain.** 

![](_page_22_Picture_6.jpeg)

The isotropic distribution of crystallites causes the scattered Xray intensity is distributed in **Debye rings**, in the same way as in powder diffraction. However, due to the strain, the rings are **deformed** in different way depending on stress status. 111

#### Residual Stress and Lattice Spacings for Grains without Strain

 $\theta_1, \theta_2, \theta_3$ 

 Crystal grains without strain.
 Every crystal grain forms the same lattice spacing d.

d

Intensity

![](_page_23_Figure_3.jpeg)

2θ

![](_page_23_Picture_4.jpeg)

grain

#### Residual Stress and Lattice Spacings for Grains with Compressive Strain

- Compressive stress applied
- The lattice spacing d decreases as the normal of lattice planes tilts from the normal of the sample surface.

![](_page_24_Figure_4.jpeg)

#### **Residual Stress and Lattice Spacings** for Grains with Tensile Strain

![](_page_25_Figure_2.jpeg)

#### Sin<sup>2</sup>ψ method

![](_page_26_Figure_2.jpeg)

#### Sin<sup>2</sup> $\psi$ method — uni-axial stress measurement method

#### (1) Measurement conditions of Sin<sup>2</sup>ψ method

- A sufficient number of crystallites exists in the area irradiated by Xrays.
- ② Stress induced in the specimen is bi-axial ( $\sigma_{33}=\sigma_{23}=\sigma_{13}=0$ ).
- ③ No stress distribution does exist within the X-ray penetration depth.
- ④ No strong texture does exist in the specimen.
- (5) The dependence of the 2 $\theta$  on sin<sup>2</sup> $\psi$  is defined by a straight line.

The inclination angle of the line is used to calculate stress value.

#### (2) Advantage of the sin<sup>2</sup>ψ method

Residual stress can be obtained without using the accurate diffraction angle  $2\theta_0$  of undistorted lattice planes !

![](_page_27_Picture_11.jpeg)

![](_page_27_Figure_12.jpeg)

![](_page_28_Figure_1.jpeg)

## **Stress Sensitivity**

The following equation is derived from the derivative of the Bragg's equation ( $\lambda$ =2d sin $\theta$ ). When the strain  $\varepsilon$  is constant, the larger  $\theta$  gives the larger  $\Delta \theta$ , which is half of the peak shift caused by the residual stress. Thus, reflections in the high diffraction angles  $2\theta$  are very sensitive to stress!

## $\varepsilon = -\Delta\theta \cot\theta$

 $\begin{bmatrix} \epsilon & : \text{ strain } (=(d-d_0)/d_0)^* \\ * \text{ d and } d_0 \text{ are the lattice spacings with and without strain, respectively.} \\ 2\theta & : \text{ Diffraction angle} \end{bmatrix}$ 

![](_page_29_Picture_7.jpeg)

#### **Lattice Planes Used for Residual Stress Measurement**

Sample	Lattice constant (Å)	Characteristic X-ray	Lattice plane	Diffraction angle (°)
α-Fe		CrKα	(211)	156.08
(Ferrite、Martensit)	2.8664	CoKα	(310)	161.35
γ-Fe	2 656	CrKβ	(311)	149.6
(Austenite)	3.000	CrKα	(220)	128.9
AI and allays	4.049	CrKα	(222)	156.7
		<b>CoK</b> α	(420)	162.1
		<b>CoK</b> α	(331)	148.7
		CuKα	(333)	164.0
Cu	3.6153	CrKβ	(311)	146.5
		<b>CoK</b> α	(400)	163.5
		CuKα	(420)	144.7
WC	2.9062	<b>CoK</b> α	(211)	165.8
	2.8378	CuKα	(301)	146.76
Ti	2.950	<b>CoK</b> α	(114)	154.6
	4.686	<b>CoK</b> α	(211)	142.3
		CuKα	(302)	148.7
Ni	3.5238	CrKβ	(311)	157.7
		CuKβ	(420)	155.6
Cr	2.8845	CrKα	(211)	153.0
		<b>CoK</b> α	(310)	157.5

![](_page_30_Picture_3.jpeg)

## Non-linearity of $sin^2\psi$ -20 diagram

![](_page_31_Figure_2.jpeg)

For anisotropic and nonuniform polycrystals, the  $\sin^2 \psi$  method does not permit to calculate the components of the stress tensor, however, the curves  $\varepsilon^{hkl}_{\psi\varphi}(sin^2\psi)$ are helpful to investigate qualitatively the distribution of the stresses in the sample, for example, presence of stress gradient or texture

Typical shapes of  $\sin^2\psi$ - $\epsilon$  diagrams

![](_page_31_Picture_5.jpeg)

## Non-linearity of $sin^2\psi$ -20 diagram

Non-linearity of  $\sin^2\psi$ -20 diagrams can be complemented by increasing number of  $\psi$  points, where the non-linearity is caused by texture, stress gradient along the depth direction and shear stress components  $\sigma_{13}$  and  $\sigma_{23}$ .

![](_page_32_Figure_3.jpeg)

Non-linearity of  $\sin^2\psi$ -2 $\theta$  diagrams

![](_page_32_Picture_5.jpeg)

#### **Strain and Stress tensors: Hook's law**

Strains and stresses both form 2<sup>nd</sup> rank tensors, each having 9 components. Due to the symmetry,  $s_{ij} = s_{ji}$  and  $e_{ij} = e_{jj}$ :

$$\sigma = \begin{pmatrix} \sigma_{11} & \sigma_{12} & \sigma_{13} \\ \sigma_{21} & \sigma_{22} & \sigma_{23} \\ \sigma_{31} & \sigma_{32} & \sigma_{33} \end{pmatrix} \qquad \qquad \varepsilon = \begin{pmatrix} \varepsilon_{11} & \varepsilon_{12} & \varepsilon_{13} \\ \varepsilon_{21} & \varepsilon_{22} & \varepsilon_{23} \\ \varepsilon_{31} & \varepsilon_{32} & \varepsilon_{33} \end{pmatrix}$$

Generalized Hook's low connects strain and stress tensors via 4-rank stiffness tensor  $c_{ijkl}$  or compliance tensor  $s_{ijkl}$ , each with 81 components (36 independent due to symmetry)

$$\sigma_{ij} = c_{ijkl} \varepsilon_{kl} \qquad \qquad \varepsilon_{ij} = s_{ijkl} \sigma_{kl}$$

For materials with isotropic elastic properties, the Young modulus E and Poisson ratio v connect stress and strain:

$$\sigma_{11} = E\varepsilon_{11} + \nu(\sigma_{22} + \sigma_{33}) \qquad \sigma_{12} = \frac{E\varepsilon_{12}}{(1+\nu)}$$
  

$$\sigma_{22} = E\varepsilon_{22} + \nu(\sigma_{11} + \sigma_{33}) \qquad \sigma_{13} = \frac{E\varepsilon_{13}}{(1+\nu)}$$
  

$$\sigma_{33} = E\varepsilon_{33} + \nu(\sigma_{22} + \sigma_{11}) \qquad \sigma_{23} = \frac{E\varepsilon_{23}}{(1+\nu)}$$

![](_page_33_Picture_8.jpeg)

#### **Stress states**

Uniaxial: all except one diagonal components are zero:

$$\sigma_{ij} = \begin{bmatrix} \sigma_{11} & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{bmatrix} \text{ or } \sigma_{ij} = \begin{bmatrix} 0 & 0 & 0 \\ 0 & \sigma_{22} & 0 \\ 0 & 0 & 0 \end{bmatrix} \text{ or } \sigma_{ij} = \begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & \sigma_{33} \end{bmatrix}$$

Biaxial: all non-zero components are located at single plane:

$$\sigma_{ij} = \begin{bmatrix} \sigma_{11} & \sigma_{12} & 0 \\ \sigma_{21} & \sigma_{22} & 0 \\ 0 & 0 & 0 \end{bmatrix}$$

Biaxial with shear: except  $\epsilon_{\scriptscriptstyle 33}$  all components are non-zero:

$$\sigma_{ij} = egin{bmatrix} \sigma_{11} & \sigma_{12} & \sigma_{13} \ \sigma_{21} & \sigma_{22} & \sigma_{23} \ \sigma_{31} & \sigma_{32} & 0 \end{bmatrix}$$

Triaxial: all components are non-zero

$$\sigma_{ij} = \begin{bmatrix} \sigma_{11} & \sigma_{12} & \sigma_{13} \\ \sigma_{21} & \sigma_{22} & \sigma_{23} \\ \sigma_{31} & \sigma_{32} & \sigma_{33} \end{bmatrix}$$

![](_page_34_Picture_10.jpeg)

## **Fundamental equation**

Using the Hook's law, the measured strain  $\varepsilon_{\psi\phi}$  at Bragg reflection *hkl* is connected to stress via so-called **fundament equation** for residual stress (isotropic case)

![](_page_35_Picture_3.jpeg)

$$\begin{aligned} {}^{hkl}_{\psi\phi} &= \frac{1}{2} S_2 \sin^2 \psi [\sigma_{11} \cos^2 \phi + \sigma_{12} \sin 2\phi + \sigma_{22} \sin^2 \phi - \sigma_{33}] \\ &+ \frac{1}{2} S_2 \sin 2\psi [\sigma_{13} \cos \phi + \sigma_{23} \sin \phi] + S_1 (\sigma_{11} + \sigma_{22}) + \sigma_{33} (\frac{1}{2} S_2 + S_1). \end{aligned}$$

where X-ray Elastic Constants (XEC):

$$S_1 = -\frac{\nu}{E}; \quad \frac{1}{2}S_2 = \frac{1+\nu}{E}.$$

Fundamental equation contains 6 unknown stress tensor components. They can be found as a solution of the system of linear equations obtained from the measurement of strain at 6 different angles  $\psi$  and  $\varphi$ .

The values of the diagonal and non-diagonal components of the strain tensor may differ essentially, and thus even small errors in the measured positions of the diffraction peaks make the analysis unstable. Therefore, the analytical  $\sin^2 \psi$  method is used.

![](_page_35_Picture_9.jpeg)

## **Inducing Residual Stress in a Sample**

![](_page_36_Figure_2.jpeg)

![](_page_36_Picture_3.jpeg)

# Analysis of stress distribution along the depth direction

Electrical polishing allows us to observe the residual stress along the depth direction.

Example of a sample with shot-peening process

![](_page_37_Figure_4.jpeg)

![](_page_37_Picture_5.jpeg)

#### **Iso-inclination method and Side-inclination method**

![](_page_38_Figure_2.jpeg)

 $N'(at \psi)$  : Normal of the lattice planes

![](_page_38_Figure_4.jpeg)

## **Optical System of Stress Measurement**

![](_page_39_Figure_2.jpeg)

aaku

![](_page_39_Picture_3.jpeg)

#### **PDXL software: Stress**

![](_page_40_Figure_2.jpeg)

![](_page_40_Picture_3.jpeg)